

## Estimating Joint Health State Utility Algorithms Under Partial Information

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### Abstract:

**Objectives** We explored the performance of existing joint health state utility estimators when data are not available on utilities that isolate single-condition health states excluding any co-occurring condition.

**Methods** Using data from the National Epidemiologic Survey on Alcohol and Related Conditions-III, we defined 2 information sets: (1) a full-information set that includes the narrowly defined health state utilities used in most studies that test the performance of joint health state utility estimators, and (2) a limited information set that includes only the more broadly defined health state utilities more commonly available to researchers. We used an example of alcohol use disorder co-occurring with cirrhosis of the liver, depressive disorder, or nicotine use disorder to illustrate our analysis.

**Results** We found that the performance of joint health state utility estimators is appreciably different under limited information than under full information. Full-information estimators typically overestimate the joint state utility, whereas limited-information estimators underestimate the joint state utility, except for the minimum estimator, which is overestimated in all cases.

**Conclusions** Researchers using joint health state utility estimators should understand the information set available to them and use methodological guidance appropriate for that information set. We recommend the minimum estimator under limited information based on its ease of use, consistency (and therefore a predictable direction of bias), and lower root mean squared error.

**Keywords:** combining | comorbidity | quality of life | utility

### Article:

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## Preference-Based Assessments

# Estimating Joint Health State Utility Algorithms Under Partial Information

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## ABSTRACT

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## Introduction

Cost-effectiveness analysis (CEA) is a standard element of establishing the evidence base in healthcare.<sup>1,2</sup> CEA provides a quantitative measure of value by simultaneously comparing the costs and outcomes of one intervention to those of another. Best practice guidelines<sup>1,2</sup> recommend that quality-adjusted life-years be used as the outcome measure in CEA, resulting in cost-utility analysis. Quality-adjusted life-years combine both the length of life and quality of life as measured with health utility, which ranges from 0 (for dead) to 1 (for perfect health) and captures the individuals' preferences for living in discrete health states. Best practice guidelines<sup>1,2</sup> also recommend that health utilities be measured using generic, preference-based measures. Although these measures may not isolate the discrete health state in question, they are often used to define the average health utility associated with a discrete health state in Markov or other state transition models.

Estimating health utility for a health state defined by a single health condition is relatively straightforward but becomes more complicated when 2 or more health conditions co-occur.<sup>3–6</sup> Estimating health utility for so-called “joint health states” is particularly critical for health conditions that commonly co-occur

with other conditions or for treatments in which adverse events are common or serious,<sup>3,7,8</sup> such as impotence after the treatment of prostate cancer<sup>9,10</sup> or comorbid mental health and substance use disorders.<sup>11–13</sup> In these cases, ignoring the utility loss associated with the joint health state can bias CEA results and lead to faulty policy recommendations.

Although the preferred approach is to use empirically estimated utilities for joint health states,<sup>8,14</sup> the number of possible joint states often makes this impractical. Theoretically-derived estimation algorithms have, therefore, been proposed to estimate joint health state utilities using the utilities of the relevant single health states, and a growing literature explores how well these algorithms perform in estimating the true joint health state utility.<sup>15</sup>

From a theoretical standpoint,<sup>16</sup> a joint health state should be a combination of the attributes that define each of the underlying single health states. Thus, the utility of a joint health state can be assessed using the same stated preference elicitation methods that are used to estimate the utility of single health states. These methods describe health states based on their underlying attributes and assess the utility of any given health condition, or combination of any multiple health conditions, based on the stated preferences for living in such states. Theory predicts that a

health state with more negative attributes should have lower utility than a state with fewer negative attributes. By definition, a joint health state has more negative attributes than either of the associated single-condition health states and so should have a lower utility than either single-condition health state. Comparing the utility of the joint health state to the utility of the associated single-condition states, therefore, allows researchers to test key theoretical assumptions, the assessment methods used, or both.<sup>17,18</sup>

Although the theoretical anchoring of joint health state utility estimators has many advantages, it results in estimation algorithms that may require more information than is commonly available to researchers using generic, preference-based measures. These measures capture data on the health state attributes included in the measure, and not necessarily the attributes most salient for the underlying health conditions. Furthermore, joint health state utility estimators require information on the utility of each single-condition health state with no comorbidities, and possibly the health state defined by the absence of both health conditions under consideration. Yet, utilities for single-condition health states are more commonly reported for anyone with that health condition, regardless of any other condition they may have. Thus, it can be difficult to find estimates of the “pure” single-condition health state utilities required by most joint health state estimation algorithms.

This article explores the performance of joint health state utility estimators when only limited information is available. We used data from the National Epidemiologic Survey on Alcohol and Related Conditions-III (NESARC-III) on the health utility associated with alcohol use disorder (AUD) and select co-occurring conditions to empirically test the performance of 4 joint health state utility estimators and to provide practical guidance on the conditions under which each estimator is likely to be optimal.

## Background

Four joint health state utility estimators have been investigated by the field<sup>15</sup>:

1. the minimum estimator, in which the lesser of 2 single states' utilities is used as an estimate of their joint utility<sup>16</sup>;
2. the additive or constant decrement estimator, in which the sum of the 2 single states' disutilities (ie, 1 - utility) is subtracted from a baseline utility to estimate their joint utility (to a minimum of 0)<sup>19</sup>;
3. the multiplicative estimator, in which the product of the 2 single states' utilities is used as an estimate of their joint utility<sup>16</sup>; and
4. the adjusted decrement estimator, a nonparametric model that combines the 2 single states' utilities in proportion to the difference between them.<sup>6</sup>

A fifth estimator, the linear index estimator,<sup>3</sup> has been proposed but is less commonly used. The linear index estimator is a parametric model that uses the weighted sum of the minimum and maximum of the 2 single states' utilities and their interaction to estimate the joint state's utility.<sup>3,20</sup> The optimal weights for the linear index estimator seem to be specific to the health conditions in question<sup>15,20</sup> and so it is difficult to implement in practice.

Studies have explored the practical application of these algorithms for estimating joint health state utilities.<sup>3,5-7,9,11,14,17</sup> Most studies use data from large databases that include a preference-weighted quality-of-life measure and data on a variety of health conditions experienced by sample members. Such data can be used to estimate the mean health utility of individuals with a joint

health condition as well as that of individuals with each of the pure single health conditions comprising the joint condition. Using the mean utility of the pure single health states, the authors predict the joint health state utility using one or more joint state utility estimators and compare the predicted joint state utility to the directly estimated joint state utility. Based on their review of the literature, Ara and Wailoo<sup>15</sup> recommend the multiplicative estimator; a recommendation that is supported by more recent research<sup>20</sup> and by a recent ISPOR task force.<sup>8</sup>

A key practical consideration this literature has identified is the appropriate choice of baseline utility.<sup>15</sup> Theoretically, the absence of all adverse health conditions should result in a health utility of 1; and so, many algorithms for estimating the utility of a joint health state initially used a baseline of 1 as the utility of having neither condition. However, the absence of the 2 health conditions in question does not imply the absence of other possible health conditions that might impact health utility (except in the case of direct utility elicitation wherein such perfect health can be described). As a result, a baseline other than 1 is more appropriate, such as the age-adjusted health utility of those with neither of the conditions under consideration or the age-adjusted health utility of the general population if more granular data are not available.<sup>8,15</sup>

## Empirical Issue

An empirical issue that has not yet been explored in the literature is the impact of not using pure single-condition utilities in joint state utility predictors. If researchers collect or have access to appropriate individual-level data, they can estimate the pure single-condition utilities, and quite possibly the joint health state utility as well. More commonly, researchers use data from published estimates of the mean utility among individuals with the conditions in question,<sup>8</sup> resulting in a much more limited information set that does not include the pure single-condition utilities. When published estimates of utility for a health condition are used, the “single-state” utility is typically the mean utility across all individuals with the health condition in question, with limited information on any other health conditions they may have. Thus, researchers using population-level estimates often do not know the pure single-condition utilities.

More specifically, consider 2 health conditions, A and B, and define terms as population means, as detailed in [Table 1](#). We define these terms as population-level means, not directly observed individual-level utilities because population means are more commonly available. We also define 2 information sets: a

**Table 1.** Health state utility notation definitions.

Utility notation	Definition
$U_{ALL}$	Mean utility of all individuals
$U_A$	Mean utility of all individuals with condition A
$U_B$	Mean utility of all individuals with condition B
$U_{nA}$	Mean utility of all individuals without condition A
$U_{nB}$	Mean utility of all individuals without condition B
$U_{AnB}$	Mean utility of individuals with condition A but not B
$U_{BnA}$	Mean utility of individuals with condition B but not A
$U_{nAnB}$	Mean utility of individuals with neither health condition
$U_{AB}$	Mean utility of individuals with both conditions A and B

**Table 2.** Joint health state utility estimation algorithms under full and partial information.

Estimator	Full-information algorithm	Limited information	
		Algorithm	Expected bias
Minimum	$\min(U_{AnB}, U_{BnA})$	$\min(U_A, U_B)$	$(1 - p_{B A})(U_{AnB} - U_{AB})$ , if $U_A < U_B$ $(1 - p_{A B})(U_{BnA} - U_{AB})$ , if $U_B < U_A$
Additive	$U_{nAnB} - [(U_{nA} - U_{AnB}) + (U_{nB} - U_{BnA})]$	$U_{ALL} - [(U_{ALL} - U_A) + (U_{ALL} - U_B)]$	$(1 - p_{B A})(U_{AnB} - U_{AB}) - (U_{ALL} - U_B)$
Multiplicative	$U_{nAnB} \frac{U_{AnB}}{U_{nA}} \frac{U_{BnA}}{U_{nB}}$	$U_{ALL} \frac{U_A}{U_{ALL}} \frac{U_B}{U_{ALL}}$	$(1 - p_{B A}) \frac{U_B}{U_{ALL}} U_{AnB} - (1 - p_{B A}) \frac{U_B}{U_{ALL}} U_{AB}$
Adjusted decrement	$\min(U_{AnB}, U_{BnA}) - \min(U_{AnB}, U_{BnA}) [(1 - U_{AnB})(1 - U_{BnA})]$	$\min(U_A, U_B) - \min(U_A, U_B) [(1 - U_A)(1 - U_B)]$	$(1 - p_{B A})ZU_{AnB} - (1 - p_{B A}Z)U_{AB}$ , if $U_A < U_B$ $(1 - p_{A B})ZU_{BnA} - (1 - p_{A B}Z)U_{AB}$ , if $U_B < U_A$ $Z = 1 - (1 - U_A)(1 - U_B)$

full-information set and a limited-information set. The full-information set includes at least the minimal information set needed to implement joint health state algorithms as theoretically derived and as tested in most of the methodological literature:  $U_{nA}$ ,  $U_{nB}$ ,  $U_{AnB}$ ,  $U_{BnA}$ , and  $U_{nAnB}$ . The limited-information set includes data only on  $U_{ALL}$ ,  $U_A$ , and  $U_B$ . For ease of discussion, we will refer to  $U_{nA}$ ,  $U_{nB}$ ,  $U_{AnB}$ ,  $U_{BnA}$ , and  $U_{nAnB}$  as full-information utilities and  $U_{ALL}$ ,  $U_A$ , and  $U_B$  as limited-information utilities.

Our premise is that researchers more commonly have the limited-information set, and seldom have the full-information set without also knowing the joint health state utility,  $U_{AB}$ . Although we acknowledge the possibility of an intermediary-information set, in which the researcher has some additional information beyond  $U_{ALL}$ ,  $U_A$ , and  $U_B$ , we contend that it is unlikely that a researcher could know  $U_{nA}$ ,  $U_{nB}$ ,  $U_{AnB}$ ,  $U_{BnA}$ , and  $U_{nAnB}$  without also knowing  $U_{AB}$ , in which case there would be no need to use an algorithm to predict the joint health state utility.

There are both theoretical and empirical relationships among these utilities. Theoretically,  $U_{AnB}$  is a function of the attributes of health condition A only, and  $U_{BnA}$  is a function of the attributes of health condition B only. Because  $U_{AB}$  is a function of the attributes of both health condition A and health condition B, it should be a combination of the attributes determining  $U_{AnB}$  and  $U_{BnA}$ . More importantly, there is no reason a priori to assume any precise mathematical relationship among these utilities. Thus, other than suggesting  $U_{AnB} > U_{AB}$  and  $U_{BnA} > U_{AB}$ , this theoretical relationship provides no evidence of the potential performance of joint health state utility estimators. Furthermore, although aggregate data are often used to estimate the theoretical relationship among the health states, this relationship is fundamentally defined at an individual level.

The empirical relationship among these health states differs from the theoretical relationship primarily because it exists at a population level. Empirically, the mean utility of all individuals with condition A and the mean utility of the subset of individuals with the joint condition AB depends on the proportion of people in the joint state and the pure single-state AnB. Specifically,

$$U_A = p_{B|A}U_{AB} + (1 - p_{B|A})U_{AnB}$$

where  $p_{B|A}$  is the proportion of all people with condition A that also have condition B. As the prevalence ( $p_{B|A}$ ) of the joint condition increases, the joint state utility plays an increasingly important role in determining the utility among all people with condition A. In other words, as  $p_{B|A}$  increases,  $U_A$  becomes a better estimate of  $U_{AB}$  until, at  $p_{B|A} = 1$ ,  $U_A = U_{AB}$ . The relationship between the mean utility of all people with condition A and the joint health state also depends on the difference in utility between the

joint condition (AB) and the single-condition health state (AnB). The smaller the difference in utility among the health states, the less important the joint health state is in determining the overall health state utility: as  $(U_{AnB} - U_{AB})$  gets smaller,  $U_A$  becomes a better estimate of  $U_{AB}$  until, at  $(U_{AnB} - U_{AB}) = 0$ ,  $U_A = U_{AB} = U_{AnB}$ . Analogous relationships hold for  $U_B$  and suggest that, under limited information, the relative performance of joint health state estimators will vary based on the prevalence of the joint condition and the relative utility of the 2 conditions.

Using our notation, we define algorithms for estimating joint health state utilities under full and limited information, as detailed in Table 2. Based on these algorithms and the relationships in equation (1), we can derive the expected bias of each estimator (ie, the predicted joint utility minus  $U_{AB}$ ) under limited information, also detailed in Table 2.

Several important insights emerged from evaluating the expected bias of the estimators. First, in every case the bias is a weighted average of the full-information health state  $U_{AnB}$  (or  $U_{BnA}$ ) and the joint state, with the weight being a function of the prevalence of the joint state,  $p_{B|A}$  (or  $p_{A|B}$ ). Although relevant for all estimators, the bias formulas for the minimum estimator clearly illustrate the importance of  $p_{B|A}$  and  $(U_{AnB} - U_{AB})$ . It is also clear that the minimum will always overestimate the joint health state utility—that is, have a positive bias. The bias of the additive estimator starts with the same weighted average as the minimum bias but adjusts it additively based on the utility decrement associated with the comorbid condition, making clear the importance of the baseline utility ( $U_{ALL}$  in our algorithm) in determining the bias of the additive estimator. Because they use proportional utility decrements, both the multiplicative and adjusted decrement estimators adjust the weighting used in the average rather than subtracting an adjustment like the additive estimator. The extent to which these adjustments under or overcompensate for the positive bias of the minimum estimator depends on the relative utilities of the baseline and conditions A and B, but it is possible for the additive, multiplicative, and adjusted decrement estimators to underestimate the joint state utility under limited information.

## Methods

To empirically estimate the performance of the 4 joint utility estimators under limited information, we compared the predicted joint state utility to the observed joint state utility for AUD and 3 comorbid conditions: cirrhosis, depressive disorder, and nicotine use disorder.

We used data from NESARC-III, a nationally representative survey of the civilian noninstitutionalized US population, aged 18

or older, including persons living in noninstitutional group quarters.<sup>21</sup> NESARC-III classifies respondents as having AUD based on the Alcohol Use Disorder and Associated Disabilities Interview Schedule-5 (AUDADIS-5).<sup>22</sup> Individuals are classified into mild, moderate, or severe AUD in the past 12 months or before the past year. For this analysis, we defined AUD as lifetime AUD, combining mild, moderate, and severe for the past 12 months and before the past year. We estimated health utility using the 6-dimensional health state short form (SF-6D), a community-perspective measure of health utility<sup>23-25</sup> available from the 12 item short form, version 2 (SF-12v2) in the NESARC-III.

NESARC-III also collects data on medical, mental health, and substance use conditions. Medical conditions in the past 12 months are self-reported by respondents as having been “diagnosed by a doctor or other health professional.” We used a self-reported diagnosis of cirrhosis of the liver in the past 12 months as our measure of cirrhosis. We measured depressive disorder as an AUDADIS-5 lifetime diagnosis of major (disorder, episodic), dysthymic, manic, or hypomanic depression or any combination thereof. We measured nicotine use disorder as an AUDADIS-5 lifetime diagnosis of a nicotine use disorder, regardless of severity.

We chose AUD as the primary health condition (ie, condition A) because it is a prevalent and costly health condition with a high incidence of comorbid conditions,<sup>26-29</sup> and numerous alcohol intervention trials have focused specifically on comorbid conditions.<sup>30-38</sup> Using utility and prevalence estimates from the NESARC-III, we chose our 3 comorbid conditions to explore the empirical implications of the prevalence of comorbidity ( $p_{B|A}$ ) and the potential health utility impact of the comorbidity ( $U_{AnB} - U_{AB}$ ). Although commonly associated with AUD,<sup>28,39</sup> a self-reported diagnosis of cirrhosis is rare among those with a lifetime history of AUD in the NESARC-III (small  $p_{B|A}$ ) but has a large impact on utility (large  $U_{AnB} - U_{AB}$ ). In contrast, depressive disorder is moderately common among those with AUD in the NESARC-III (moderate  $p_{B|A}$ ) and has a large impact on utility (large  $U_{AnB} - U_{AB}$ ). Finally, nicotine use disorder is very common among those with AUD (large  $p_{B|A}$ ) but has a small impact on utility (small  $U_{AnB} - U_{AB}$ ). We did not explore a condition with small  $p_{B|A}$  and small  $U_{AnB} - U_{AB}$  because such a condition would be less empirically relevant.

We estimated each of the 9 mean health utilities defined above for lifetime AUD and each comorbid condition (cirrhosis, depressive disorder, and nicotine use disorder). For each joint state and under each information set, we estimated the relevant mean health utilities and used them to derive the joint state utility using each estimator, and then compare the estimator-derived joint state utility with the observed joint state’s mean utility.

We assessed the performance of the 4 estimators under limited information on the criteria of bias and root mean square error (RMSE). Bias reflects how closely the predicted value matches the observed; it is defined as the predicted mean using the estimator minus the observed mean. RMSE reflects how precise the predicted value is in matching the observed; it is defined as the square root of the mean of the squared prediction error. These performance criteria inform how “right” an estimator is and how “good” it is at prediction. Using parametric bootstrapping<sup>40</sup> that incorporates the sampling design and weights in the NESARC-III, we created 1000 bootstrap replicates for each estimator’s joint utility and calculated the mean bias for each estimator, the 95% confidence interval (CI) for the bias, and the RMSE. An estimator with a mean bias of 0 would be considered unbiased. The magnitude of the RMSE is relative to the mean and so does not have a threshold value for assessing the performance of an estimator; nevertheless, a smaller RMSE indicates a more precise estimator and so is preferred. All analyses were conducted using Stata Version 17 (StataCorp LLC, College Station, TX). Stata code to replicate our analyses is provided in the

Appendix in [Supplemental Materials](https://dx.doi.org/10.1016/j.jval.2022.09.009) found at <https://dx.doi.org/10.1016/j.jval.2022.09.009>.

## Results

Table 3 presents the unweighted sample size and the weighted mean utility and 95% CI for all health states, and the key terms from the expected bias formulas [ $p_{B|A}$ ,  $p_{A|B}$ , ( $U_{AnB} - U_{AB}$ ), and ( $U_{BnA} - U_{AB}$ )] in Table 2. The mean utility among the general population (ie,  $U_{ALL}$ ) was 0.788. The lifetime AUD (ie,  $U_A$ ) had a mean utility of 0.762; all 3 comorbid conditions (ie,  $U_B$ ) had a lower mean utility than AUD, with the lowest being associated with cirrhosis.

Table 4 presents the 4 joint health state estimators for each of the comorbid conditions under both full and limited information. As expected, the minimum estimator overestimated the joint health state utility in all cases, but less so under limited information. The additive and multiplicative estimators overestimated the joint health state utility under full information but underestimated it under limited information. The adjusted decrement estimator always underestimated the joint health state utility. This underestimation was worse under limited information than under full information.

Table 5 presents bootstrap results for the limited-information estimators and Figure 1 presents these results graphically. For cirrhosis, which had the lowest conditional prevalence but the highest utility impact, the 95% CI for the bias included 0 for all estimators. The difference between the upper and lower confidence bounds and the RMSE, however, reveals that all estimators were very imprecise. This is illustrated in the relatively broad empirical distribution of the bias for the AUD and cirrhosis joint estimators shown in Figure 1. In contrast, the joint health state estimators for depression and nicotine use disorder were much more precise. For both conditions, the 95% CIs excluded 0 across all estimators and so all were biased: the minimum was biased upwards whereas all other estimators were biased downwards. Across all conditions, the adjusted decrement estimator had the highest RMSE, whereas the minimum estimator had the lowest RMSE for all conditions except cirrhosis.

## Discussion

This article explored joint health state utility estimation using a limited-information set that assumes researchers only know the mean health utility of people with each of the conditions, with no information on other conditions they may have, if any. We also defined a full-information set that included the mean utility among samples defined by the presence and absence of each of the conditions, yielding the “pure” single-condition utilities called for in most joint utility estimators.

We found that the available information set has potentially important effects on the performance of joint utility estimators. Under full information, all estimators except the adjusted decrement estimator overestimated the joint health state utility. In contrast, under limited information, all estimators except the minimum estimator underestimated the joint health state utility. This behavior results from the full-information set using “pure” health states that isolated each of the single-state health conditions. In contrast, the “single” state utilities used in the limited-information set included both individuals in the “pure” single-state conditions and the joint condition. Thus, despite having less precise information on health states, the limited-information set included data on the joint state utilities that the full-information set intentionally excluded. The inclusion of the joint health state utility caused the underestimation of the joint

**Table 3.** Health state utilities.

	Unweighted n	Mean utility (SF-6D)	95% CI	
Limited-information health states				
General population	36 163	0.788	0.785-0.790	
Lifetime AUD	9974	0.762	0.758-0.767	
Cirrhosis	130	0.641	0.605-0.677	
Depressive disorder	4772	0.670	0.665-0.676	
Nicotine use disorder	7278	0.738	0.733-0.743	
Full-information health states				
No AUD	26 189	0.798	0.795-0.801	
No cirrhosis	35 891	0.788	0.785-0.791	
No depressive disorder	31 391	0.805	0.802-0.807	
No nicotine use disorder	28 885	0.800	0.797-0.803	
AUD, no cirrhosis	9868	0.763	0.759-0.768	
AUD, no depressive disorder	7907	0.787	0.783-0.791	
AUD, no nicotine use disorder	6218	0.782	0.778-0.787	
Cirrhosis, no AUD	72	0.655	0.604-0.707	
Depressive disorder, no AUD	2705	0.679	0.672-0.686	
Nicotine use disorder, no AUD	3522	0.751	0.744-0.758	
No AUD, no cirrhosis	26 023	0.799	0.795-0.802	
No AUD, no depressive disorder	23 484	0.811	0.808-0.814	
No AUD, no nicotine use disorder	22 667	0.805	0.802-0.808	
Joint health states				
AUD and cirrhosis	58	0.622	0.564-0.679	
AUD and depressive disorder	2067	0.659	0.652-0.666	
AUD and nicotine use disorder	3756	0.728	0.721-0.734	
Key terms from expected bias formulas in Table 2*				
	$P_{B A}$	$P_{A B}$	$(U_{AnB} - U_{AB})$	$(U_{BnA} - U_{AB})$
AUD and cirrhosis	0.005	0.438	0.142	0.034
AUD and depressive disorder	0.192	0.469	0.128	0.013
AUD and nicotine use disorder	0.532	0.366	0.061	0.023

AUD indicates alcohol use disorder; CI, confidence interval; SF-6D, six-dimensional health state short form.

\*Assumes AUD is condition A and the other conditions listed are condition B.

**Table 4.** Joint health state estimators under full and limited information.

	AUD and cirrhosis		AUD and depressive disorder		AUD and nicotine use disorder	
	Full information	Limited information	Full information	Limited information	Full information	Limited information
Observed	0.622		0.659		0.728	
Minimum	0.654	0.641	0.679	0.670	0.751	0.738
Additive	0.630	0.616	0.675	0.645	0.740	0.713
Multiplicative	0.634	0.621	0.675	0.649	0.741	0.715
Adjusted decrement	0.602	0.586	0.633	0.618	0.710	0.692

AUD indicates alcohol use disorder.

**Table 5.** Bias and RMSE of joint health state estimators under limited information.

	AUD and cirrhosis			AUD and depressive disorder			AUD and nicotine use disorder		
	Bias	95% CI	RMSE	Bias	95% CI	RMSE	Bias	95% CI	RMSE
Minimum	0.021	−0.040 to 0.084	0.037	0.011	0.003 to 0.012	0.012	0.011	0.003 to 0.018	0.011
Additive	−0.005	−0.063 to 0.059	0.032	−0.014	−0.024 to −0.005	0.015	−0.015	−0.024 to −0.005	0.015
Multiplicative	−0.000	−0.058 to 0.063	0.031	−0.011	−0.019 to −0.001	0.012	−0.013	−0.022 to −0.004	0.014
Adjusted decrement	−0.034	−0.095 to 0.030	0.047	−0.042	−0.050 to −0.033	0.042	−0.035	−0.043 to −0.027	0.035

AUD indicates alcohol use disorder; CI, confidence interval; RMSE, root mean squared error.

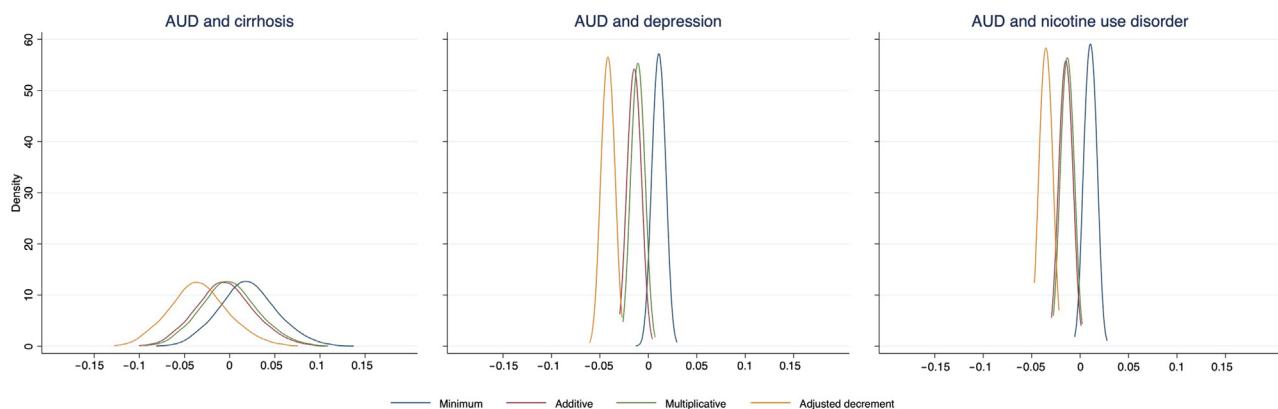
health state utility under limited information, and its exclusion caused overestimation under full information.

When we compared the empirical performance of the 4 estimators under limited information, we found that the minimum had the best performance based on RMSE. This conclusion is somewhat undermined by the performance of the minimum estimator in the very rare comorbidity of cirrhosis, but we contend that the better RMSE for depression and nicotine use disorder outweighed the performance for cirrhosis. Across all conditions, we conclusively eliminated the adjusted decrement estimator as defined in the literature. The adjusted decrement estimator was the only estimator that used 1 as the baseline utility. It is well established that this baseline causes an underestimation of joint state utilities because it overstates the decrement in utility associated with the single-condition health states.<sup>15</sup> We speculate that the performance of the adjusted decrement estimator may improve if another baseline utility is considered. The additive and multiplicative estimators were surprisingly similar in all cases, despite recommendations that the multiplicative is preferred under full information.<sup>8,15,20</sup> The expected bias formulas detailed in Table 1 reveal that the relative performance of these estimators is driven more by the difference in the utility decrement relative to the baseline than by the prevalence of the joint condition. Our empirical evidence suggests that large differences in the relative utility decrement are needed to create an appreciable difference in performance between the additive and multiplicative estimators under limited information.

### Limitations

Our results are based on a single data set, using a single utility measure, and focused on a single clinical area. Analyses using data from a different population, a different utility measure, or focusing on a different clinical area may yield different results. Furthermore, our study focused on the utility of joint health states defined by 2 co-occurring health conditions and so may not extend to joint health states defined by 3 or more conditions. Studies using full-information utilities to explore joint health states defined by 3 or more conditions<sup>20</sup> suggest that our results may not hold; future research could extend our work to assess the performance of joint health state estimators in such circumstances.

In addition, our inclusion of cirrhosis as a co-occurring condition is debatable given its very low sample size in the NESARC-III. Nevertheless, its low sample size is why it offers an interesting point of comparison. From a clinical perspective, relatively rare concurrent conditions may be important to include. Indeed, rare conditions can be very expensive and, thus, have important implications for resource allocation. Thus, researchers need guidance on how to include rare conditions in a CEA. Furthermore, our use of cirrhosis reflects the possibility that a concurrent condition may be common among those with a specific condition but not well measured in epidemiological data: research suggests that 20% of heavy drinkers will develop cirrhosis<sup>28</sup> but that it is undiagnosed in 69% of those with cirrhosis.<sup>39</sup> Thus, we feel it offers information on a possibly important analytical scenario.

**Figure 1.** Empirical distribution of bias for joint health state estimators under limited information.

AUD indicates alcohol use disorder.

## Conclusions

Our analysis revealed that researchers using joint health state utility estimators need to understand the information set they have at their disposal. In most cases, researchers will either have empirical data on the joint health state or be forced to use limited-information health states—meaning those utilities that do not isolate single-condition health states to exclude the presence of any co-occurring condition—to estimate the joint health state utility. All estimators performed differently under partial information than under full information. The joint utility estimator literature is dominated by studies that assume full-information utilities are available yet use the mean of a preference-based measure that captures all conditions experienced by the respondent when testing the empirical performance of varying estimators. Additional studies on this issue are needed and current methodological guidance needs to be reconsidered. In the absence of these additional studies, we recommend using the minimum of the single-state utilities as the joint health state utility estimate. The minimum has 3 distinct advantages: first, it is precise, as indicated by its relatively low RMSE; second, it has a consistent upward bias, which makes correction predictable; and third, it is easy to implement, explain, and understand, which is an important consideration for practitioners and decision-makers. Although we found all other estimators underestimated the joint health state in our empirical work, the analytical derivation of their bias revealed that this need not always be the case; the lack of a clear a priori direction of bias for estimators complicates interpretation and potentially confidence in results. The preferred approach is, of course, to use empirically estimated utilities for joint health states, which are becoming increasingly available in the peer-reviewed literature.<sup>11,41–43</sup> But when these estimates are not available, it is imperative that researchers understand the information set they have available to them and follow the guidance that is consistent with that set.

## Supplementary Material

Supplementary data associated with this article can be found in the online version at <https://dx.doi.org/10.1016/j.jval.2022.09.009>.

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