Non-renewable resource prices: Deterministic or stochastic trends?

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ABSTRACT

In this paper, we examine temporal properties of 11 natural resource real price series from 1870 to 1990. Recent studies by Ahrens and Sharma [Trends in natural resource commodity prices: deterministic or stochastic? J. Environ. Econom. Manage. 33(1997)59–74], Berck and Roberts [Natural resource prices: will they ever turn up? J. Environ. Econom. Manage. 31(1996)65–78], and Slade [Grade selection under uncertainty: least cost last and other anomalies, J. Environ. Econom. Manage. 15(1988)189–205], among others, find that many non-renewable resource prices have a stochastic trend. We revisit this issue by employing a Lagrangian multiplier unit root test that allows for two endogenously determined structural breaks with and without a quadratic trend. Contrary to previous research, we find evidence against the unit root hypothesis for all price series. Our findings support characterizing natural resource prices as stationary around deterministic trends with structural breaks. We additionally show that both pre-testing for unit roots with breaks and allowing for breaks in the forecast model can improve forecast accuracy. Overall, the results in this paper are important in both a positive and normative sense; without an appropriate understanding of the dynamics of a time series, empirical verification of theories, forecasting, and proper inference are potentially fruitless.

1. INTRODUCTION

An important literature has developed recently that empirically examines non-renewable natural resource price paths and investigates whether they are trend- or difference-stationary. For example, Ahrens and Sharma [2] use annual data on 11 commodity price series ranging from 1870 to 1990 and conclude that six of these series are stationary around a deterministic trend, while the remaining five display stochastic trends implying a unit root. In a related paper, Berck and Roberts [5] use a subset of the same data and find overwhelming support for non-stationary unit roots. Slade [32] and Abgeyegbe [1], among others, find similar overwhelming support for non-stationary natural resource prices. A consistent theme across much of this literature is that most natural resource prices are non-stationary.

Our motivation in this paper is to further the boundaries of econometric methodologies and provide new insights into natural resource price time paths. Previous empirical work on natural resource prices typically neglects possible structural change in the time series. Since the seminal work of Perron [25], it is well known that ignoring structural change in unit root tests will lead to a bias against rejecting the unit root null hypothesis when it should in fact be rejected (e.g., see also [3]). In this study, we advance the literature on time paths of natural resource prices by endogenously determining structural breaks and extending the two-break Lagrangian multiplier (LM) unit root test of Lee and Strazicich [16] to include a quadratic trend. Given that a quadratic trend might exist in some natural resource price series we believe that allowing for a quadratic trend in conjunction with structural breaks may provide additional insights.

Understanding the nature of resource price time paths is important for several reasons. Theoretically speaking, Ahrens and Sharma [2, p. 61], for example, note that in regards to both a simple and more general Hotelling [11] model as described in Slade [32], "price movement is still systematic and may be modeled appropriately as a deterministic trend." In contrast, in a world with uncertainty "in which speculative motives drive the behavior of extracting firms or unanticipated events largely characterize the market, resource prices may be generated by a random walk process" [2, pp. 61–62]. Thus, knowing the correct time series behavior of natural resource prices can be vital to distinguish among theories that most accurately describe observed behavior.

Knowledge of the time series properties of natural resource prices is also important for proper econometric estimation. For example, Ahrens and Sharma [2] and Labson and Crompton [14] note that conventional regression analysis and hypothesis testing cannot be correctly undertaken without first understanding characteristics of the time series. Otherwise, results from estimating regression models may be rendered invalid. Several additional examples can be found in the literature (see, e.g., [9]).

Finally, given that good policymaking typically depends on sound economic forecasts, appropriately modeling the nature of the time series can be invaluable to forecasters [8]. This task recently came to hand in Berck and Roberts [5], who did not consider structural breaks. They found that each commodity price series had a unit root and hence initially paid more credence to their ARIMA forecasts. Berck and Roberts [5], however, found that their ARMA forecasts outperformed their ARIMA counterparts. In the later part of our paper, we investigate

whether pre-testing for unit roots with structural change can help to identify the most accurate forecasting model. This question has not been previously examined in the literature.

Our investigation begins by examining annual data comprised of 11 fuel and metal real price series ranging from 1870 to 1990.[1] After including structural breaks, we find evidence *against* a unit root in each of the 11 series. We then estimate different forecasting models and find that ARMA models with breaks generally outperform ARIMA models with breaks, which is consistent with our pre-test expectations. These results help to solve the puzzling results noted by Berck and Roberts [5], and demonstrate the importance of considering structural breaks in economic forecasting. A second major finding is that our unit root test results are robust-with or without quadratic trends natural resource prices are stationary around deterministic trends with two structural breaks in intercept and trend slope. Thus, while nonlinear time trends are important in certain price series, rejection of the underlying unit root hypothesis and support for trend-break stationary price series does not depend on inclusion of such trends. Finally, we find that both pre-testing for unit roots and including structural breaks can improve the accuracy of forecasting natural resource prices.

The remainder of the paper is structured as follows. Section 2 provides a brief background on unit root tests and further describes the importance of understanding the time-series properties of exhaustible resource prices. Section 3 describes our empirical methodologies. Section 4 presents our empirical results. In Section 5, we examine how structural breaks affect the accuracy of forecasts. Section 6 concludes.

2. BACKGROUND

Recent years have witnessed an explosion of research that examines the time-series properties of economic data. An important stimulant in this time-series renaissance was Nelson and Plosser's [21] study, which applied unit root analysis to test for the stationarity of macroeconomic and financial time series. Since this seminal study, many authors have analyzed data ranging from stock prices to air pollutant emissions, with the bulk of research having clear implications theoretically as well as from a policy perspective (see, e.g., [18]). Certainly, the empirical results from many of these studies have broad implications in numerous areas of research.

Within the natural resource literature, Slade [32], Berck and Roberts [5], and Ahrens and Sharma [2], among others, discuss the notion that exogenous shocks can affect the time path of natural resource prices. These studies use a variety of unit root tests to examine time paths of commodity prices. Rejection of the unit root null supports the alternative hypothesis of a mean or trend reverting stationary series, implying that shock effects are transitory. Alternatively, failure to reject the unit root null implies a non-stationary series in which shocks have permanent effects; following a shock there is no tendency for commodity prices to revert to a stable mean or trend. The most recent of these studies [2] assumes one known or exogenously given structural break common to all commodity price series in 1929, 1939, or 1945; the other studies mentioned do not consider structural breaks.

Natural resource theory has stark predictions on the time pattern of resource prices. In fact, in his treatise on the economics of exhaustible resources, Hotelling [11] predicts that, under certain assumptions, the price of an exhaustible resource will rise at the rate of interest. But a quick glance at the majority of mineral commodity price series suggests that relative commodity prices have *declined*, rather than increased, for long periods of time. Barnett and Morse [4], who observed this seemingly anomalous pattern, concluded that scarcity was not a real problem. Although these particular results are crucial evidence against the original premise of Hotelling, modifications of the simple Hotelling model can produce predictions of falling or stagnant prices over time. For example, environmental constraints and natural resource abundance may induce price declinations [2]. Resource prices may also decrease when a backstop technology is introduced, causing an inward shift in the demand for natural resources (e.g., [10]). Technical change and an endogenous change also could produce decreasing, or U-shaped paths for relative prices (e.g., [31]). Finally, modifications of initial informational assumptions, such as knowledge of the original resource stock, can induce the model to predict price decreases (see [28], for one scenario).

3. A NEW MODELING APPROACH

In this paper, we begin our testing approach by employing the recently developed two-break LM unit root test of Lee and Strazicich [16]. One important advantage of the LM unit root test is that it is free of spurious rejections. Nunes et al. [23] and Lee and Strazicich [15] showed that the endogenous break ADF-type unit root tests are subject to spurious rejections in the presence of a unit root with break.[2] Because these tests assume no breaks under the null and derive their critical values under this assumption, rejection of the null need not imply rejection of a unit root per se, but may imply rejection of a unit root *without* break. As such, researchers may incorrectly conclude that a time series is (trend) stationary with break(s) when in fact the series is non-stationary with break(s). In contrast, rejection of the null using the LM test is unaffected by breaks. Thus, rejection of the null using the LM test unambiguously indicates a trend-stationary series with break(s).[3]

To illustrate the underlying model and LM testing procedure, we consider the following data-generating process (DGP):

(1)

$$y_t = \delta' Z_t + e_t,$$

(2)

$$e_t = \beta e_{t-1} + u_t,$$

where y_t is the commodity price in period t, δ is a vector of coefficients, Z_t is a matrix of exogenous variables, and u_t is an error term. We define $Z_t = [1, t, D_{1t}, D_{2t}, DT_{1t}, DT_{2t}]$ to allow for a constant term, linear time trend, and two structural breaks in level and trend, where T_{Bj} denotes the time period of the breaks. Under the trend-break stationary alternative, the D_{jt} terms

describe an intercept shift in the deterministic trend, where $D_{jt}=1$ for $T_{Bj}+1 \le t \le T_{Bj}+1$, $j=1,2$, and zero otherwise; DT_{jt} describes a change in slope of the deterministic trend, where $DT_{jt}=t$ for $T_{Bj}+1 \le t \le T_{Bj}+1$, $j=1,2$, and zero otherwise.

While Berck and Roberts [5] considered an LM unit root test with quadratic trend, they did not consider structural breaks. Ahrens and Sharma [2] advance the literature by considering one structural break that is given a priori. To further advance the literature, we consider two structural breaks that are *endogenously determined* by the data. In addition, we extend the two-break LM unit root test to allow for a quadratic trend. Defining Z_t appropriately, the DGP in (1) with quadratic trend and two breaks in intercept and trend slope can be described by $Z_t=[1, t, t^2, D_{1t}, D_{2t}, DT_{1t}, DT_{2t}]$. To the best of our knowledge, this is the first paper in any field of research to consider a quadratic time trend in an endogenous break unit root test.[4]

Test statistics for the LM unit root test are obtained from the following regression:

(3)

$$\Delta y_t = \delta' \Delta Z_t + \phi \tilde{S}_{t-1} + u_t,$$

where $\tilde{S}_{t-1} = y_t - \tilde{\psi}_x - Z_t \tilde{\delta}$, $t = 2, \ldots, T$, and $\tilde{\psi}_x = y_1 - Z_1 \tilde{\delta}$. $\tilde{S}_t$ is a detrended series of y_t using the coefficients in $\tilde{\delta}$, which are estimated from the regression in first differences of Δy_t on $\Delta Z_t=[1, \Delta D_{1t}, \Delta D_{2t}, \Delta DT_{1t}, \Delta DT_{2t}]$. This procedure follows from the LM (score) principle, which imposes the null restriction. Subtracting $\tilde{\psi}_x$ makes the detrended series begin at zero so that $\tilde{S}_1 = 0$. This detrending method based on $\tilde{\delta}$ differs from that adopted in the DF type tests, where the parameter δ is estimated from the regression of y_t on Z_t in levels. Vougas [33] has shown that the LM type test using the above detrending method is more powerful than the DF type test.

Under the null hypothesis of a unit root $\varphi=0$, and under the alternative $\varphi<0$. The LM unit root test statistic is denoted as

(4)

$$\tilde{\tau} = t - \text{statistic testing the null hypothesis } \phi = 0.$$

The search for two breaks ($\lambda_j=T_{Bj}/T$, $j=1,2$) that minimize $\tilde{\tau}$ can be described by a grid search as follows:[5]

(5)

$$\text{LM}_\tau = \underset{\lambda}{\text{Inf}} \; \tilde{\tau}(\lambda).$$

Correction for autocorrelated errors in (3) is accomplished by including augmentation terms $\Delta \tilde{S}_{t-j}, j = 1, \ldots, k$, as in the standard ADF test. To determine k we follow the "general to specific" procedure described in Perron [25]. Beginning with a maximum number of

$\Delta \tilde{S}_{t-i}$ΔS̃t-i terms, max k=8, we examine the last augmented term $\Delta \tilde{S}_{t-8}$ΔS̃t-8 for significance at the 10% level (asymptotic normal critical value is 1.645). If insignificant, the last augmented term is dropped from the regression and the model is re-estimated using k=7k=7 terms, etc., until the maximum lagged term is found or k=0k=0, at which point the procedure ends. We repeat this procedure at each combination of two break points $\lambda=(\lambda_1,\lambda_2)'$λ=(λ1,λ2)′ over the time interval [0.1T, 0.9T] (to eliminate end points).[6]

4. EMPIRICAL RESULTS

Our data, generously provided by W. Ashley Ahrens and Vijaya Sharma, are annual real price series for 11 fuels and metals. The series are typically available from 1870 to 1990 and include aluminum, bituminous coal, copper, iron, lead, nickel, petroleum, natural gas, silver, tin, and zinc.[7] To allow a direct comparison with previous research, we use commodity price series similar to those examined in Slade [32] and Berck and Roberts [5], and, of course, identical to the data used in Ahrens and Sharma [2].[8] Visual inspection of each time series in Fig. 1 suggests that most are stationary with one or two structural breaks. In a few series, there is evidence suggesting a possible nonlinear (quadratic) trend. Curvature of trend would be consistent with Hotelling's basic premise. Yet, in Fig. 1, the trends are not typically convex with a positive first derivative—a majority of the figures show that relative commodity prices have *declined* rather than increased. This finding matches results in previous studies and casts doubt on some predictions of the simple Hotelling [11] model.
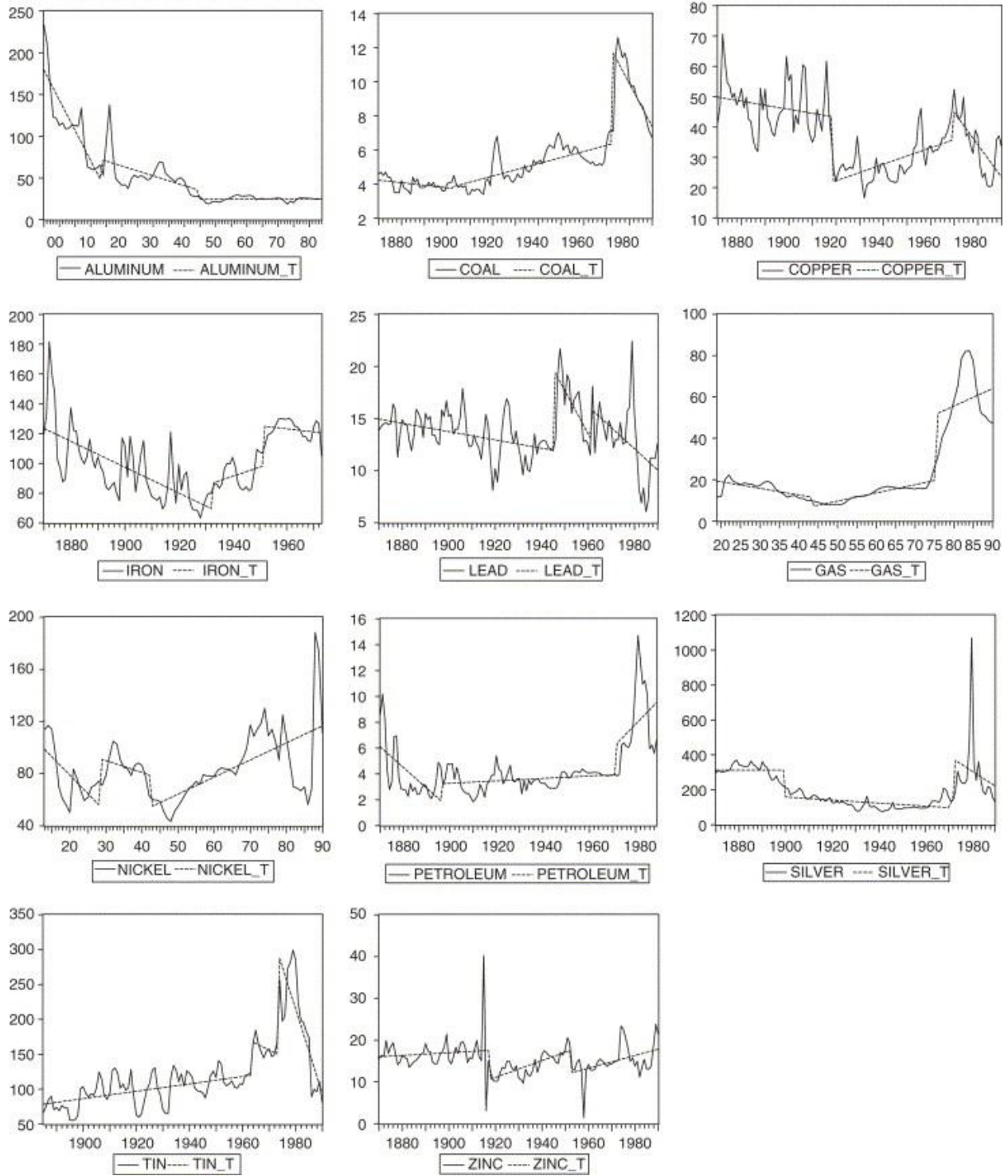
Fig. 1. Plot of data with structural breaks and fitted trends.

Although casual inspection of Fig. 1 provides some insights, formal econometric tests are necessary to determine the properties of each time series. In our analysis, we strive for the most

general results possible. Accordingly, we employ five different unit root tests to analyze each price series. Our first test, also employed by Berck and Roberts [5], is the no-break LM unit root test of Schmidt and Phillips [29, SP hereafter] with an added quadratic time trend. Our second test is the two-break LM unit root test developed in Lee and Strazicich [16]. To check the robustness of our findings, and more clearly examine the effect of including two breaks instead of one, in our third test we utilize the one-break minimum LM unit root test of Lee and Strazicich [17]. In our most general empirical model we extend the two-break LM unit root test to include a quadratic time trend. Finally, we extend the one-break LM test to include a quadratic trend. Our combination of testing procedures permits us to compare our findings with previous studies, while simultaneously allowing us to isolate effects of allowing for breaks.

4.1. QUADRATIC TREND WITH NO BREAK

Test results using the no-break SP LM unit root test with linear and quadratic time trends are presented in the fourth column of Table 1. The second column provides the sample size and the third column notes the starting year. Details of all other estimated results including estimated parameters, quadratic trend terms, the number of lagged terms included to correct for serial correlation, and critical values can be found in Table A1 in the on-line Appendix at http://www.aere.org/journal/index.html. Overall, the no-break LM test results indicate that five of the 11 real price series reject the unit root null at the $p<.05$ level (coal, iron, lead, gas, and zinc). Interestingly, four of these five series (all except lead) have a quadratic time trend that is significantly different from zero at conventional levels, whereas the six series that do not reject the unit root have insignificant quadratic time trend terms. Thus, non-rejection of a unit root hypothesis for these six series may be due to lower power caused by including an insignificant quadratic time trend, or to bias from omitting breaks. Consistent with Ahrens and Sharma [2, Table 4], our results reject the unit root in nearly half the series; but our rejections do not overlap completely. One explanation for this finding is our inclusion of a quadratic time trend—[2] do not include a quadratic trend in their ADF tests. Ahrens and Sharma [2] also employ the test suggested by Ouliaris et al. [24, OPP hereafter], which includes a quadratic time trend but no structural break. Our results still do not exactly replicate their findings. One possible explanation, which is noted by Ahrens and Sharma [2], is that the OPP test is plagued by size distortions. Fortunately, similar size distortions do not occur in the no-break SP LM test and may help to explain the difference in results.

Table 1
LM unit root test results

Series	T	Starting year	Quadratic trend (no break)	Two-break (w/linear trend)	One-break (w/linear trend)	Two-break w/quadratic trend	One-break w/quadratic trend
Aluminum	90	1895	0.88	−5.39*	−3.45	−5.15	−4.38
Coal	121	1870	−3.75**	−7.75**	−4.08	−8.51**	−6.95**
Copper	121	1870	−3.06	−6.01**	−5.18**	−6.70**	−5.33**
Iron	104	1870	−4.83**	−6.72**	−5.49**	−6.66**	−6.31**
Lead	121	1870	−4.69**	−6.91**	−5.22**	−7.30**	−5.30**
Gas	72	1919	−3.87**	−6.46**	−5.24**	−9.54**	−7.33**
Nickel	78	1913	−2.00	−5.44*	−5.08**	−6.22**	−5.27**
Petroleum	120	1870	−1.77	−5.65*	−3.82	−5.74	−5.30**
Silver	121	1870	−2.94	−7.22**	−3.84	−7.49**	−4.31
Tin	106	1885	−2.20	−6.66**	−4.97**	−6.97**	−5.56**
Zinc	121	1870	−3.74**	−10.4**	−5.96**	−10.4**	−9.38**

Column header note: "LM unit root test statistics given a model specification with:" spans the five test statistic columns.

Notes: Test statistics test the null hypothesis of a unit root. * and ** denote significant at the 10% and 5% levels, respectively. Details of all other estimated results can be found in Table A1 in the on-line Appendix at http://www.aere.org/journal/index.html

Comparing our results with those in Berck and Roberts [5], which use the same *no-break* SP LM test with quadratic trend, we find that inferences across the two sets of empirical results differ significantly. Whereas we reject the unit root in five price series, they cannot reject the unit root in any of their nine series at the 5% level. This difference in results is most likely due to the longer time series in our tests, leading to greater power to reject the null—whereas we make use of the entire data set, Berck and Roberts [5] use two smaller subsets of the data (i.e., 1940–1976 and 1940–1991). Using these shorter time series, we were able to replicate the results in Berck and Roberts [5]. We should note that replication was achieved even though they used a transformed test based on estimating the long-run variance, whereas we employed an augmented version of the no-break SP LM unit root test. This provides evidence that the difference in results is not due to different methods of correcting for autocorrelated errors.

4.2. Two endogenous breaks with a linear trend

Moving to our more flexible models, we next examine empirical results from the two-break LM unit root test with linear trend in column five of Table 1. Details of other estimated results for the two-break LM unit root test can be found in Table A2 of the on-line Appendix. The empirical results using the two-break test may well reflect the reduction in bias from including variables to model structural change. Compared to the no-break SP LM test results, we find significantly more rejections of the unit root null. Whereas the no-break model (column four) rejects the unit root null in five of 11 series at the $p<.05$ level, the two-break model rejects the unit root null in eight of 11 series at $p<.05$. If one considers a slightly less stringent $p<.10$ test, the two-break model rejects the unit root null in all 11 series. These findings provide the strongest evidence to date against the unit root process as a description of natural resource prices.

Overall, our two-break test results in column five of Table 1 strengthen the findings of Ahrens and Sharma [2], and differ from the conclusions of Agbeyegbe [1], Berck and Roberts [5], and Slade [32], among others. Whereas Ahrens and Sharma [2] allow for one known break in 1929, 1939, or 1945 and reject the unit root in five of eight price series, after allowing for two endogenously determined breaks we reject the unit root in all 11 series. By including one (known) structural break Ahrens and Sharma [2] can be seen as an extension of Berck and Roberts [5], while our tests can be seen as a further extension to a more general model.[9]

To further examine the effect of allowing for two breaks instead of one, we next test all price series using the endogenous one-break LM test with linear trend. The results are displayed in column six of Table 1.[10] Compared to the two-break results in column five, we find fewer rejections of the unit root using the one-break test (seven of 11 series reject the null at $p<.05p<.05$ and $p<.10p<.10$). This difference in results is likely due to bias from omitting the second break variable, and demonstrates the impact of allowing for two breaks instead of one.[11]

The estimated break years are summarized in Table 2. Comparing the breaks identified by the two-break LM tests with linear trend to those in Ahrens and Sharma [2], only one of our estimated break years (1945, lead) coincides exactly with an assumed break year selected by Ahrens and Sharma [2]. However, five additional breaks identified by our two-break tests (1928, 1932, 1942, 1943, and 1944) are close to one of their assumed breaks (1929, 1939, and 1945). Overall, our identified break years are intuitively appealing as they broadly correspond to years associated with World War I, the Great Depression, World War II, and the energy crisis of the early 1970s. Thirteen of the twenty-two breaks (59%) identified with the two-break test in column two correspond to these time periods, with the most common time period for breaks in the early 1970s. Besides these obvious breaks, we identify three other breaks in column two that are associated with relevant important historical events. In 1896 a structural break occurs for petroleum during the major depression of 1893–1897. In 1902 we identify a structural break for coal prices. This year coincides with the 150,000 United Mine Workers strike that crippled coal production in the USA for five and one-half months. In 1961 a structural break occurs for lead, which coincides with the Lead and Zinc Stabilization Program of the same year.

Table 2
Estimated structural break points

Series	Structural break years given a model specification with:			
	Two-break	One-break	Two-break with quadratic trend	One-break with quadratic trend
Aluminum	1913 (I) 1944 (II)	1914 (I)	1913 (I) 1942 (II)	1913 (I)
Coal	1902 (C) 1972 (E)	1915 (I)	1949 1972 (E)	1972 (E)
Copper	1918 (I) 1969	1918 (I)	1897 (D) 1970 (E)	1934 (GD)
Iron	1932 (GD) 1951	1927	1933 (GD) 1951	1951
Lead	1945 (II) 1961 (LZ)	1946 (II)	1945 (II) 1961 (LZ)	1946 (II)
Gas	1943 (II) 1975 (E)	1973 (E)	1929 (GD) 1979	1978
Nickel	1928 1942 (II)	1969	1930 (GD) 1974 (E)	1977
Petroleum	1896 (D) 1971 (E)	1896 (D)	1914 (I) 1926	1919 (I)
Silver	1899 1972 (E)	1960	1892 (S) 1972 (E)	1968
Tin	1963 1974 (E)	1969 (E)	1963 1974 (E)	1973 (E)
Zinc	1917 (I) 1952	1955	1917 (I) 1952	1917 (I)

Notes: (I) denotes in the time period of World War I; (II) denotes in the time period of World War II; (GD) denotes in the time period of the Great Depression; (E) denotes in the time period of the energy crisis of the early 1970s; (D) denotes in the time period of the 1893–1897 depression; (S) denotes the silver strike of 1892; (C) denotes the coal miners strike of 1902; and (LZ) denotes the lead and zinc stabilization program of 1961.

4.3. Two endogenous breaks with a quadratic trend

In column seven in Table 1 we present results from our most general model, the two-break LM unit root test with a quadratic time trend. Since this test is new to the literature, we follow the procedure of Lee and Strazicich [16] and simulate critical values, which are available along with other estimated results in Table A4 in the on-line Appendix.[12] Compared to the two-break test results in column five, which include only a linear trend, we report a few significant differences. Whereas exclusion of the quadratic time trend leads to rejection of the unit root at the 10% level in all 11 series (eight of 11 at $p<.05p<.05$), after including quadratic time trends, unit roots are not rejected (at the 10% level) for aluminum and petroleum. However, the results for aluminum should be interpreted with care, as the coefficient on the quadratic time trend is not significantly different from zero at conventional levels, suggesting the linear time trend specification is more appropriate. Although we find that the quadratic time trend is significant at the 10% level in five of the 11 price series (coal, copper, lead, gas, and petroleum), other results are qualitatively unchanged. Overall, at the 5% level, the results in Table 1 of the two-break test with quadratic trend suggest that we should reject the unit root in nine of the 11 series, providing additional evidence that commodity prices are stationary around a breaking deterministic trend.

To further examine the effect of allowing for two breaks instead of one, we additionally test all price series using an endogenous one-break LM test with quadratic trend.[13] The unit root test results are displayed in column eight of Table 1.[14] Compared to the two-break with quadratic trend results in column seven, we find the same number of rejections of the unit root null (nine of 11 series reject the null at $p<.05$ and $p<.10$). The only notable difference in results is with regards to the two series that do not reject the unit root. In the two-break quadratic trend results in column seven, aluminum and petroleum did not reject the unit root, but in the one-break test results of column eight petroleum rejects the unit root (at $p<.05$) while silver does not. The difference in results for silver is likely due to bias from omitting the second break variable. The difference for petroleum may be due to including an unnecessary break in the two-break quadratic trend model, which would be expected to reduce power.

The estimated break years for the two-break test with quadratic trend are summarized in column four in Table 2. The majority of identified breaks again correspond primarily to the two World Wars, the Great Depression, and the 1970s energy crisis. As in the two-break model with linear trend, 13 of the 22 breaks (59%) correspond to these time periods with the most common time period during the energy crisis of the early 1970s. Other important events noted in column four include a major silver miners strike in 1892, a break for copper during the depression of 1893–1897, and a break for lead during the Lead and Zinc Stabilization Program of 1961.

The most appropriate model in the literature to compare our results is, again, Ahrens and Sharma's [2] OPP test, which allows for a quadratic trend but no structural break(s). Using the OPP test, Ahrens and Sharma [2] reject the unit root null in five of eight series at $p<.05$ while using the two-break LM test with quadratic trend we reject the unit root in nine of 11 series at the 5% level. This difference is likely due to allowing for structural breaks.

To examine further the effects of allowing for breaks, we present plots showing each commodity price series in Fig. 1. Each panel shows the actual commodity price series as well as fitted values from a linear time trend regression connecting the two breaks in intercept and trend slope identified in Table 2 (column two). The plots in Fig. 1 suggest that most price series are trend-stationary around a small number of breaks. More importantly, a visual inspection indicates that it may be more appropriate to specify the model with discrete shifts in a deterministic linear trend rather than a quadratic trend. Even in some series for which a quadratic trend appears to fit, the linear trend model with two structural breaks also appears to fit the data well. Overall, seven of the 11 series have downward trends in the most recent period.

In sum, the above results provide the strongest evidence to date against the unit root hypothesis and suggest that natural resource price series are stationary around deterministic trends with occasional changes in intercept and trend slope. Our findings are at odds with those in previous studies. In addition, our findings strengthen those of Ahrens and Sharma [2], who concluded that the majority (six of 11) of natural resource price series reject the unit root hypothesis. In certain respects, our unit root test results

are consistent with the scores of theoretical models that suggest resource price paths are deterministic, but downward or U-shaped. In the next section, we examine how structural change affects forecasting.

5. FORECASTING ISSUES

As aforementioned, we view one contribution of the above analysis as informing the forecaster. Whether, and to what extent, structural change in natural resource prices influences the selection and performance of forecasting models is largely unknown, however. In this section we fill this void by exploring whether pre-testing for a unit root with structural change and inclusion of breaks in the forecast model can lead to more accurate forecasts. Diebold and Kilian [7] previously examined whether pre-testing for unit roots matters for forecasting, given that a priori information on the properties of a time series is not available. The issue that we examine is similar in spirit, yet we consider structural breaks. One may argue that allowing for breaks when pre-testing for unit roots can give potentially different results, since a unit root process with breaks can sometimes be viewed as observationally equivalent to, or hardly distinguishable from, a trend stationary process with breaks. Intuitively speaking, this can be the case because structural change implies persistent effects similar to those in a unit root process. Since the pioneering work of Perron [25], however, it is well known that inference in unit root tests will be adversely affected by ignoring structural change. Under the alternative hypothesis of a trend-break stationary series, structural change would be described by occasional predetermined large shocks that permanently alter the level and slope of the deterministic trend. This is the common view in the literature as consistently advocated in numerous theoretical and empirical papers. Following this view, the existence of structural change is not considered to be sufficient support for the unit root hypothesis.

In this section, we seek to determine how structural change will affect the selection and accuracy of forecasting models when we do not know a priori if a time series is (trend) stationary (with breaks) or non-stationary (with breaks). Several authors have noted the deleterious effects of ignoring structural breaks in forecasting models (see, e.g., [27], [26] and [6]). However, these previous papers deal with mostly stationary data and do not address the question of whether forecasts in levels perform better than forecasts in differences in the presence of breaks.

We begin our investigation by conducting Monte Carlo simulations to study the role of structural breaks in selecting and estimating the most accurate forecasting model. To do so, we compare the unconditional prediction mean squared error (PMSE) of the following five strategies:

> (M1) Difference the data and include two breaks in intercept and trend slope.
>
> (M2) Analyze the data in levels and include two breaks in intercept and trend slope.

(M3) Pre-test with unit root tests that allow for two breaks in intercept and trend slope and proceed as follows: if the unit root null is rejected, then select M2; if we cannot reject the unit root, then select M1.

(M4) Difference the data and do not allow for breaks.

(M5) Analyze the data in levels and do not allow for breaks.

Note that models M1–M3 are conditional on the existing breaks, while M4 and M5 are not. Thus, we can compare the performance of pre-testing for a unit root in addition to the effect of including known breaks in the forecasting model. In general, when comparing the accuracy of forecasts with different models the common approach is to compare out-of-sample forecasts. We follow this approach.[15]

For simplicity, we restrict our simulations to AR(1) or ARI(1,1) models as in Diebold and Kilian [7]. Thus, M1 is an ARI(1, 1) model with two breaks and can be described as follows:

(6)

$$\Delta y_t = \mu + b\Delta y_{t-1} + d_1 B_{1t} + d_2 B_{2t} + d_3 D_{1t} + d_4 D_{2t} + v_t,$$

where $B_{jt} = 1$ for $t = T_{Bj} + 1$, $j = 1, 2$, and zero otherwise. Note that M1 uses differenced data with two one-time break dummy variables (B_{jt}) and two level shift dummy variables (D_{jt}). In contrast, M2 is an AR(1) model in levels with two breaks in level and trend as follows:

(7)

$$y_t = c + by_{t-1} + d_1 D_{1t} + d_2 D_{2t} + \gamma t + d_3 DT_{1t} + d_4 DT_{2t} + w_t,$$

where D_{jt} and DT_{jt} denote the level and trend shift dummy variables, respectively. Note that M2 also includes a time trend, which is differenced away in M1. M3 would be either M1 or M2 as in the model in (6) or (7) depending on the results from pre-testing for a unit root (with two breaks). On the other hand, M4 and M5 do not allow for structural breaks. M4 uses the differenced data without breaks in the forecasting model, while M5 uses the level data without breaks. Thus, M4 and M5 can be described by (6) and (7), respectively, without the dummy variables describing the breaks. We will now examine these different forecasting models by using simulations.

To generate simulated data we use the following equation, which is similar to the DGP in (1):

(8)

$$(y_t - c - \gamma t - d_1 D_{1t} - d_2 D_{2t} - d_3 DT_{1t} - d_4 DT_{2t}) = \beta(y_{t-1} - c - \gamma(t-1) - d_1 D_{1,t-1} - d_2 D_{2,t-1} - d_3 DT_{1,t-1} - d_4 DT_{2,t-1}) + u_t.$$

With (8), we can generate both stationary and non-stationary data with and without breaks. To generate non-stationary data we let $\beta=1.0$, while to generate stationary data we let $\beta=0.95$ and $\beta=0.5$. We can control the magnitude of the breaks by varying the coefficients of the dummy variables. To generate the data without breaks, we set the break coefficients in (8) equal to zero. One interesting question is how big should structural breaks be to be recognized as such? We will examine this question by varying the magnitude of the break coefficients:

$d=(d_1, d_2, d_3, d_4)=(0,0,0,0), (2,2,0.2,0.2), (6,6,0.6,0.6)$, and $(10, 10, 1.0, 1.0)$. To abbreviate in Table 3, we will denote these break magnitudes as $d=0$, $d=2$, $d=6$, and $d=10$, respectively, where $d=0$ indicates the model without breaks. All break sizes are described using standardized units. We additionally consider different break locations at $T_{B1}/T=0.3$ and $T_{B2}/T=0.6$. Other parameter values are held fixed in all cases; we let $c=0$, $\gamma=0.1$, and $\sigma_u^2=1$.

Table 3
Simulation results comparing the forecast accuracy of different strategies

d	h	$T=100$											
		$\beta=1.0$				$\beta=0.95$				$\beta=0.5$			
		M1/M3	M2/M3	M4/M3	M5/M3	M1/M3	M2/M3	M4/M3	M5/M3	M1/M3	M2/M3	M4/M3	M5/M3
0	1	0.99	1.10	0.98	1.02	0.99	1.07	0.97	0.98	1.14	0.99	1.12	0.94
	5	0.99	1.21	0.92	1.07	0.99	1.19	0.89	0.95	1.46	0.97	1.35	0.80
	10	1.00	1.21	0.87	1.06	0.99	1.19	0.81	0.87	1.51	0.97	1.29	0.72
	50	1.00	1.27	0.66	0.97	1.00	1.34	0.46	0.56	1.74	0.94	0.81	0.36
	100	1.00	1.34	0.57	1.31	0.99	1.45	0.30	0.47	1.83	0.93	0.56	0.19
2	1	0.99	1.14	0.99	1.01	0.99	1.12	0.98	0.99	1.13	1.00	1.14	1.18
	5	0.99	1.27	1.00	1.07	0.99	1.22	0.97	1.02	1.48	0.97	1.62	1.95
	10	0.99	1.25	1.02	1.09	0.99	1.20	0.97	1.00	1.54	0.97	2.20	2.97
	50	1.00	1.25	1.06	1.27	1.00	1.32	1.11	1.00	1.76	0.93	9.38	6.29
	100	1.00	1.30	1.07	2.33	1.00	1.43	1.28	1.42	1.88	0.92	14.75	7.25
6	1	0.98	1.47	1.10	0.99	0.97	1.42	1.09	0.98	1.10	0.99	1.26	1.14
	5	0.99	1.52	1.60	1.07	0.98	1.43	1.60	1.04	1.53	0.97	3.66	1.60
	10	0.99	1.36	2.12	1.15	0.99	1.29	2.22	1.11	1.58	0.97	9.17	1.69
	50	1.00	1.21	4.21	1.88	1.00	1.24	6.26	1.84	2.00	0.94	77.61	2.30
	100	1.00	1.22	5.07	2.83	0.99	1.30	9.00	2.87	2.21	0.92	127.1	2.86
10	1	0.95	2.17	1.26	0.97	0.95	1.99	1.26	0.96	1.04	1.00	1.41	1.08
	5	0.98	1.77	2.75	1.12	0.99	1.62	2.79	1.11	1.52	0.98	7.43	1.68
	10	0.99	1.45	4.27	1.30	0.99	1.35	4.57	1.26	1.63	0.97	22.79	2.10
	50	1.00	1.20	10.22	2.66	1.00	1.24	16.43	3.04	2.11	0.94	215.1	11.11
	100	1.00	1.20	12.93	4.11	1.00	1.28	24.70	5.36	2.34	0.93	350.1	23.07

Note: Results with $T=500$ are available in the on-line Appendix at http://www.aere.org/journal/index.html. The results with $T=500$ reinforce the above results.

To undertake our comparisons we examine the recursive one-step ahead predictions of y_{T+h} at forecast horizons h ranging from 1 to 100 periods, and employ a sample size of $T=100$.[16] Pre-testing is performed using the two-break LM unit root test and critical values at the 5% level

of significance. To compare the forecast accuracy of each model, we calculate the ratio of the PMSE for each h in each model relative to the PMSE of the reference pre-test strategy M3. The calculated ratios are denoted as M1/M3, M2/M3, M4/M3, and M5/M3. For the models estimated in first-differences, the forecasted values are converted to levels prior to calculating their mean squared error. The forecast error is calculated as the difference between the (simulated) data and the predicted values (in levels), or $y_{T+h} - \hat{y}_{T+h}$, $h = 1, \ldots, 100$.

$$\mathrm{PMSE}(h) = h^{-1} \sum_{j=1}^{h} (y_{T+j} - \hat{y}_{T+j})^2$$

Thus, $\mathrm{PMSE}(h) = h^{-1} \sum_{j=1}^{h} (y_{T+j} - \hat{y}_{T+j})^2$ using forecast errors through $t = h$. When the selected forecasting model is more accurate than the model suggested by pre-testing, then the ratio will be less than one and vice versa. For parsimony, we report only the summary results for selected values of h.

We first examine the simulation results using non-stationary data ($\beta = 1.0$) in Table 3. When the DGP is non-stationary, the differencing strategy of M1 (ARI with breaks) has the lowest PMSE in nearly all cases. There are only very small differences in some cases. In nearly all cases the best model (M1) is also the model that is selected by the pre-testing. Any differences are approximately zero, and the results are unaffected by the size of the breaks. Overall, these results clearly support the use of pre-testing for a unit root and including structural breaks. For the case of no breaks there is a small gain from omitting the breaks in the (differenced) forecasting model (M4). For the case of small breaks ($d = 2$), the results demonstrate little difference between including breaks (M1) and omitting breaks (M4). Thus, as one might expect, small breaks have only minimal effects on the PMSE and can be hardly considered as structural breaks. However, as the size of the breaks increases the benefit of including breaks increases especially at longer forecast horizons.

We next examine the simulation results using stationary data in Table 3. When the DGP is clearly stationary ($\beta = 0.5$), the model in levels with breaks (M2) is superior in virtually all cases. Any differences are so small that they are approximately zero and can be ignored. In addition, M2 is the model that is selected with pre-testing in nearly every case. Again, any differences are quite small, and the results are unaffected by the break size and forecast horizon. When $\beta = 0.95$ and the unit root null is more difficult to reject, the most accurate forecasting model is in differences (M1) instead of levels (M2). However, the difference model is also the model most frequently selected by pre-testing. Thus, pre-testing for a unit root with breaks is again the preferred method to select the most accurate forecasting model. As in the non-stationary case, including breaks when they exist is always beneficial. Fig. 2 and Fig. 3 summarize the simulation results by displaying spectrum with varying sample sizes of $T = 20n$, $n = 1, \ldots, 50$, over the continuum of forecasting horizons $h = 1, \ldots, 100$. These figures generalize the results in Table 3 and are consistent with the above discussion.
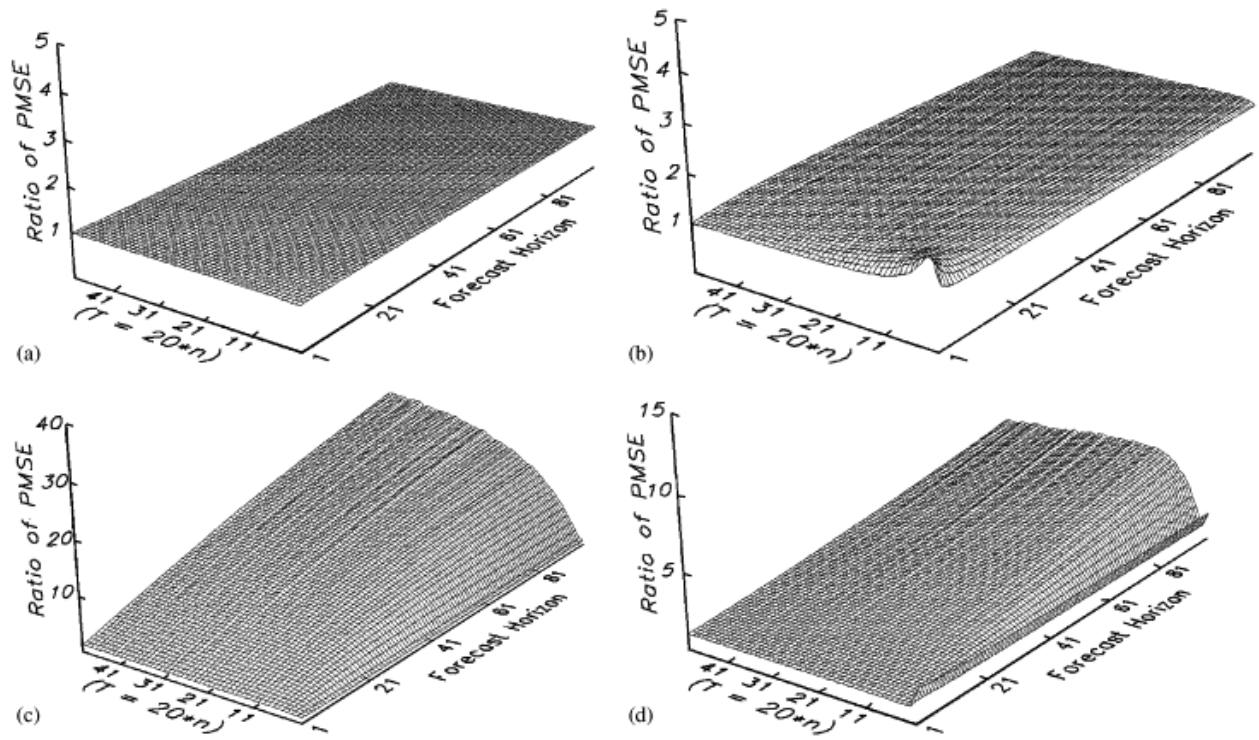
Fig. 2. Comparison of forecast accuracy using different strategies (DGP: $\beta=1\beta=1$, $d=6d=6$): (a) difference with breaks (M1/M3); (b) level with breaks (M2/M3); (c) difference without breaks (M4/M3); (d) level without breaks (M5/M3).
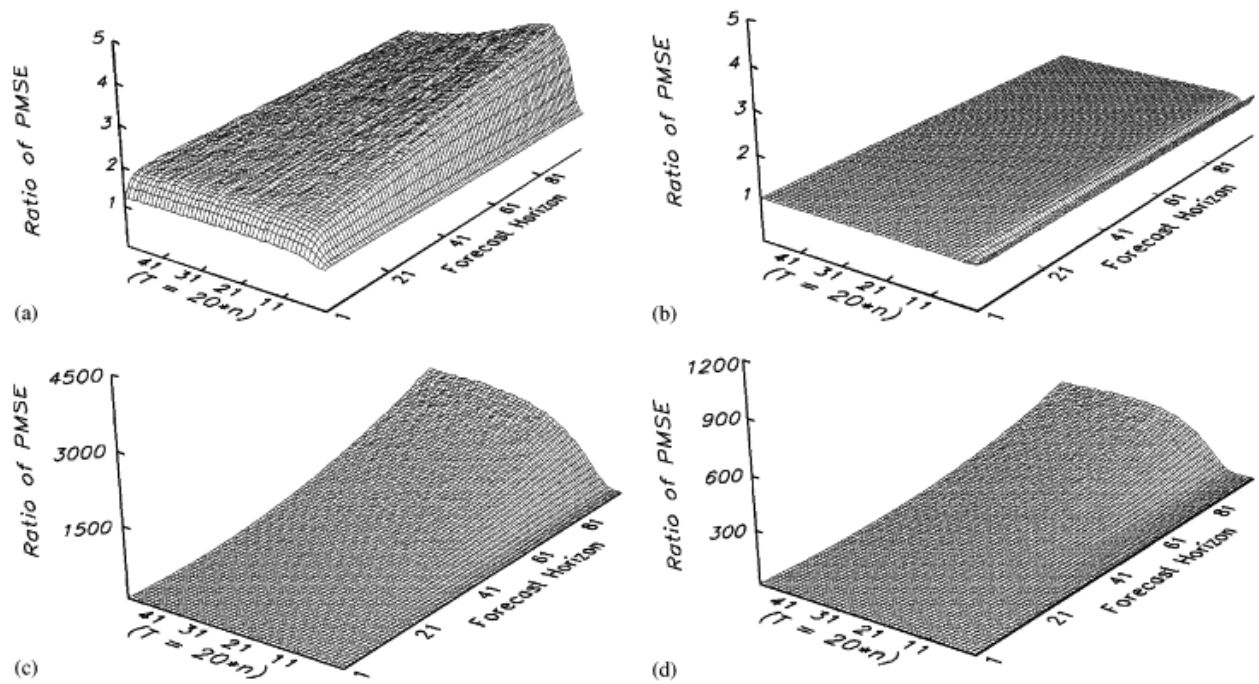

Fig. 3. Comparison of forecast accuracy using different strategies (DGP: $\beta=0.5\beta=0.5$, $d=6d=6$).

To further our investigation, we next examine and compare the accuracy of the different forecasting strategies by using actual data on natural resource prices. To perform our investigation, we utilize more recent data on eight natural resource real prices (aluminum, copper, iron, lead, nickel, silver, tin, and zinc). These data come from the US Geological Survey [13], and are available annually from 1900 to 2002 in real (1998) dollars per ton.[17]

Our testing procedure is as follows. We first perform pre-testing for each real price series as before using the two-break LM unit root test with linear trend. In nearly all cases (except for nickel), the unit root null is rejected at the 10% level of significance. We also perform pre-testing using the two-break LM unit root test with quadratic trend and reject the unit root in all cases at the 10% level of significance.[18] Next, we estimate four forecasting models for each series with a linear trend as in (6) and (7) (M1, M2, M4, and M5), and then with a quadratic trend (M1Q, M2Q, M4Q, and M5Q).

Instead of the AR(1) and ARI(1, 1) models (with and without breaks) considered in the simulations of Table 3, we consider more general ARMA(p,q) and ARIMA(p, 1, q) models that might be more realistically considered in applications. To determine the order p and q of each ARMA and ARIMA model, and the location of two breaks, we utilize the SBC statistic. We consider all combinations of p and q over the range 0–5 at each combination of two breaks to find the model with the lowest SBC. As such, our estimation procedure allows for the location of breaks to be jointly determined with the best fitting model. In each case, we estimate the forecasting model using data from 1900 to 1990 and generate out-of-sample forecasts in levels for 1991–2002.[19] Then, the out-of-sample forecasts are compared to the actual data to calculate the relevant PMSE. To test the statistical significance of the break variables in the models that include breaks, F-tests were performed to test for the significance of the breaks. In each case, the null hypothesis that break coefficients are jointly equal to zero was rejected at the 1% level of significance. These results provide additional evidence that structural breaks are important.

The PMSE are displayed in Table 4 for each model type at forecast horizons h=1h=1, 3, 5, 8, and 12. The number in bold denotes the model with the most accurate forecasts (smallest PMSE), which is shown separately for the models with linear and quadratic trends. At each forecast horizon (h), the best overall model is denoted with an asterisk (*). Given that pre-testing implied that price series are trend-break stationary, we expect that M2 (ARMA model in levels with breaks) will have the lowest PMSE in nearly all cases.

Table 4
Comparison of post-1990 PMSE using different models with actual data

(All prices in 1998$ per ton)	h	Linear trend				Quadratic trend			
		M1	M2	M4	M5	M1Q	M2Q	M4Q	M5Q
Aluminum ($000)	1	688	472*	656	497	995	716	2368	2168
	3	432	192*	277	236	1883	1235	3642	3108
	5	299	226*	386	383	1989	1018	3522	2908
	8	339	215*	532	588	3289	1182	4402	3583
	12	718	215*	1055	948	6095	1588	6111	4966
Copper ($000)	1	278	1*	135	69	158	265	2	437
	3	768	8*	539	477	931	498	385	2273
	5	554	285*	377	419	773	333	303	2000
	8	1085	246*	583	1003	1289	550	837	4114
	12	1958	228*	921	1960	2334	774	1899	7051
Iron ($)	1	13	0*	24	88	0	1	18	25
	3	23	1*	148	195	3	1	46	118
	5	87	26	281	315	43	15*	60	206
	8	347	155	382	401	186	87	53*	295
	12	758	342	476	631	371	176	77*	508
Lead ($000)	1	245	99	366	32*	156	152	194	126
	3	355	74*	704	204	166	171	251	186
	5	346	48*	853	179	136	156	232	214
	8	293	33*	962	164	102	166	194	167
	12	291	22*	1207	210	120	314	220	165
Nickel ($000,000)	1	5	19	1*	3	1	4	22	36
	3	23	89	46	9*	18	25	108	106
	5	107	310	50	9*	83	104	77	97
	8	287	816	72	9*	228	278	110	114
	12	685	1922	98	9*	550	657	135	141
Silver ($000,000,000)	1	0.666	0.359*	4.96	5.89	0.392	0.752	21.03	46.65
	3	4.83*	5.48	9.74	13.28	5.97	5.85	61.79	196.42
	5	16.56	19.60	8.24*	13.27	21.26	19.59	86.70	334.38
	8	42.00	45.29	7.94*	15.89	49.48	43.55	120.81	446.32
	12	84.74	87.58	9.19*	22.06	96.44	81.72	167.59	371.39
Tin ($000,000)	1	2	19	0*	2	16	1	0	10
	3	6	69	3	16	68	16	2*	16
	5	19	103	4	20	150	45	1*	39
	8	47	199	7	35	332	81	1*	69
	12	99	348	15	60	668	155	1*	122
Zinc ($000)	1	305	246	271	28*	239	295	170	523
	3	345	475	435	50*	362	452	303	1120
	5	358	447	518	80*	457	524	375	1386
	8	366	474	592	69*	561	584	468	1576
	12	487	640	814	139*	854	783	753	1892

Notes. PMSE is the predicted mean squared error of the post-1990 out-of-sample forecast period (h). M1 = differences with breaks, M2 = levels with breaks, M4 = differences without breaks, M5 = levels without breaks, and Q denotes that the model includes a quadratic trend. Structural breaks were jointly significant in all models that included breaks at $p<0.01$. * Denotes the model with the lowest PMSE.

We now examine the results in Table 4. Except for tin, and to a lesser extent iron, we see little evidence that including a quadratic trend improves the accuracy of the forecast, as the best model has a linear trend in all other cases. For aluminum, copper, and lead our pre-test expectations are realized as the most accurate model in every case but one (lead, $h=1h=1$) is

the ARMA model in levels with breaks (M2). While iron selects the quadratic trend model at three of the five forecast horizons, three of its five best models are in levels with breaks (M2, M2Q) as suggested by the pre-test. For the other four price series the results are mixed. In all cases but one (h=1h=1), the best forecasting model for nickel is the ARMA model in levels without breaks (M5). For silver, the results are unexpected as four of the five best models are in differences (M1, M4), and three of these are without breaks (M4). Tin is the series where the quadratic trend model is most often selected (four of five best models). Although including a quadratic trend provides better forecasting accuracy for tin, the best model chosen in all cases is in differences and without breaks (M4, M4Q). Finally, zinc selects an ARMA model in levels in all cases as predicted by pre-testing, but the best model is without breaks (M5).

Overall, the results in Table 4 using actual natural resource data present a less clear picture than our simulation results in Table 3. However, as expected, the most consistently selected model is the same as selected in the pre-test; in four of the eight series the ARMA model with breaks (M2 or M2Q) is the most accurate in nearly all cases. For the other four series the results are less clear. In some of these cases, the best model is in levels as expected, but without breaks. In other cases the superior model is in differences. Thus, while the model selected by pre-testing is not always the best model it appears that pre-testing for a unit root and considering breaks are important. The gain from considering breaks is most obvious when comparing the PMSE of those superior models that include breaks to the other models.

In general, as is well known, forecasting future values out-of-sample is a difficult task. Therefore, it may not be desirable to draw any generalized conclusions regarding forecasting strategies from a particular data application to a particular out-of-sample period. Choosing different data and different out-of-sample periods may lead to different conclusions. Thus, we give stronger credence to our simulation results as a guide to more accurate forecasting. We conclude that it is better to follow a forecasting strategy of pre-testing for a unit root with breaks and to include existing breaks in the forecast model.

6. CONCLUDING REMARKS

Without an appropriate understanding of the dynamics of a time series, empirical verification of theories, forecasting, and proper inference are potentially misleading. In this paper, we examine temporal properties of 11 non-renewable natural resource real price series from 1870 to 1990. Previous efforts largely suggest that these series are difference-stationary with stochastic trends. We re-examine these data and advance the literature by considering unit root tests with two structural breaks that are endogenously determined by the data. In addition, we consider models with linear and quadratic trends.

Overall, we find evidence to indicate that natural resource prices are stationary around deterministic trends with structural breaks in intercept and trend slope. In particular, after controlling for breaks, the previous empirical findings of Agbeyegbe [1], Berck and Roberts [5], and Slade [32] are essentially reversed. Our findings strengthen those of Ahrens and Sharma [2], who allowed for one known break and concluded that the majority of natural resource price

series (six of 11) reject the unit root. Following our unit root tests, we examined forecasting models with breaks by employing both simulated and actual natural resource price data. We conclude that pre-testing for a unit root with breaks selects the best forecasting model.

Given that accurate forecasting and empirical verification of theories can depend critically on understanding the appropriate nature of time-series, our results should have important implications for academics and policymakers alike. With the proliferation of environmental and natural resource data having a temporal dimension, researchers interested in dynamic issues as broad as environmental quality expenditures, environmental degradation, species extinction rates, and land-use patterns should have a firm grounding in time-series analysis. We hope that our paper will further the development of this literature.

NOTES

1. This data was utilized to most accurately compare our empirical findings to the previous works. In Section 5, we estimate a variety of forecasting models with updated data through 2002.

2. The endogenous break ADF-type unit root tests include the one-break minimum test of Zivot and Andrews [34] and two-break minimum test of Lumsdaine and Papell [19]. These tests have been popular in the literature. However, as shown in Lee and Strazicich [16] and [17], these tests tend to estimate the break point incorrectly at one period prior to the true break(s) where bias in estimating the unit root test coefficient is greatest. The outcome is a size distortion that increases with the magnitude of the break. Due to a different detrending procedure in the endogenous break LM test, this type of size distortion does not occur.

3. As is common practice in the literature, we refer to a time series that is stationary around a breaking trend as "trend-break stationary."

4. There are technical difficulties in obtaining relevant asymptotic distributions and corresponding critical values of endogenous break unit root tests with three or more breaks. However, for our purposes, including three or more breaks does not appear necessary. First, visual inspection of the data reveals that more than two breaks are unlikely. Second, the two-break test is found to have sufficient ability to reject the unit root in all cases.

5. Note that the break locations and unit root test statistic are jointly estimated in the minimum LM unit root test. Critical values were derived given this joint estimation [16].

6. This "general to specific" procedure has been shown to perform well as compared to other data-dependent procedures in selecting the optimal number of augmented terms (see, e.g., [22]).

7. Price series for aluminum, iron, and petroleum are available through 1984, 1973, and 1989, respectively. Aluminum, gas, nickel, and tin begin in 1895, 1919, 1913, and 1885, respectively.

8. These data were previously converted to real prices by deflating with the producer price index (1967=100). Most of the data comes originally from Manthy [20] and Schurr [30].

9. An anonymous referee notes that the shorter time span (1940–1991) examined in Berck and Roberts [5] can be viewed as allowing for a structural break in 1940. However, as our results will demonstrate, while World War II is one of the major structural breaks identified by our tests, there are other breaks that we identify. By considering a longer time span of data, our testing procedure should benefit from greater power and a reduction in bias from including additional breaks. It is also possible that failure to reject the unit root null in Berck and Roberts [5] might be due to their inclusion of a quadratic trend. If a quadratic trend does not occur, especially in the post-1940 time period, then inclusion would lower power. We thank an anonymous referee for noting this possibility.

10. Details of other estimated results and critical values are in Table A3 in the on-line Appendix.

11. For comparison purposes, we also performed unit root tests using the ADF-type one-break Zivot and Andrews [34] test and two-break Lumsdaine and Papell [19] test. While these tests tend to over-reject the null, their results are similar to ours. The two-break LP test rejects the null at the 10% level for all series except for gas and petroleum. Details of these results are available upon request.

12. Since the two-break LM unit root test with quadratic trend is a new test, we derive critical values by generating pseudo-iid $N(0, 1)$ random numbers using the Gauss (version 6.0.5) RNDNS procedure. Critical values are derived using 5000 replications involving a grid search of all combinations of the endogenous break points for minimum statistics in samples of $T=100$. The asymptotic distribution of the two-break minimum LM test with quadratic trend can be shown by a simple modification of the expression for that of the two-break minimum LM test with linear trend. The expression of the demeaned and de-breaked Brownian bridge $\underline{V}(r, \lambda)$ $V(r,\lambda)$ in Lee and Strazicich [16, Eq. (6c), Appendix A.6] must be changed to incorporate a detrended p-level Brownian bridge as given in SP [29, Eq. (40)]. This expression is described as a residual process projected onto the subspace generated by $dz(\lambda, r) = [1, \underline{r}, d_1(\lambda_1, r), d_2(\lambda_1, r)]$ $dz(\lambda,r)=[1,r,d1(\lambda1,r),d2(\lambda1,r)]$. The trend function is given as $\underline{r} = \{r^j, j = 0, 1, \ldots, p - 1\}$ $r=\{rj,j=0,1,\ldots,p-1\}$, where $d_j(\lambda_j, r) = 1$ $dj(\lambda j, r)=1$ if $r > \lambda_j$ $r > \lambda j$, for $j=1,2$ and 0 otherwise.

13. We thank an anonymous referee who suggested this robustness check.

14. Details of other estimated results and critical values are in Table A5 in the on-line Appendix.

15. There does not appear to be a unanimous consensus on this issue, however. Inoue and Kilian [12] suggest that comparing in-sample tests of forecast accuracy are more reliable than out-of-sample tests. The underlying issue is potential data mining or un-modeled structural change. Also, the accuracy of out-of-sample forecasts can depend on the selection of the holdout period.

16. Simulation results for sample sizes $T=500$ are available in Table A6 in the on-line Appendix.

17. We would have preferred to update our data, but the new data uses a different PPI to deflate and different units of measurement. In addition, the new data is only available for eight of our previous 11 natural resource price series. However, besides using more recent data (past 1990), the new data has the advantage that each series is available for the same time period.

18. These results are available upon request.

19. As noted in footnote 15, the out-of-sample PMSE results might vary depending on how we define the out-of-sample period. We also considered 1996 as a starting period for the out-of-sample forecasts, but the main conclusions did not vary.

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